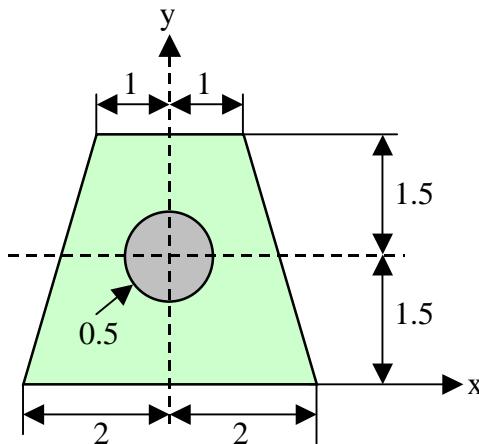


AREA MOMENT OF INERTIA

Problem 4:

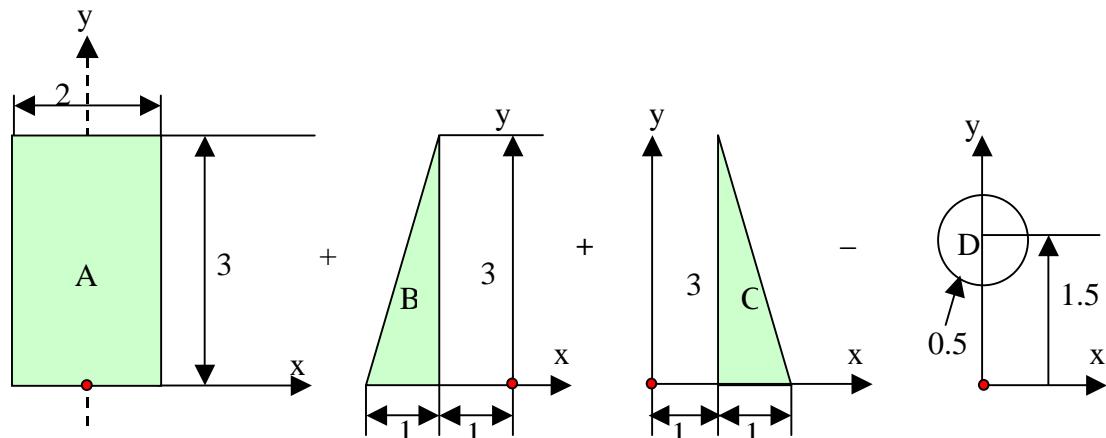
Determine the area moment of inertia of the composite area about

- a) the x-axis
- b) the y-axis



Solution:

The composite area consists of 4 component parts:



| Part | Area, A | d_x | d_y | Ad_x^2 | Ad_y^2 | I_{xo} | I_{yo} |
|-----------------|--------------------------|--------|--------|--------------|----------|---------------------------------|---------------------------------|
| Unit | (in^2) | (in) | (in) | (in^4) | (in^4) | (in^4) | (in^4) |
| A | $3(2)=6$ | 1.5 | 0 | 13.5 | 0 | $(2)(3)^3/12= 4.5$ | $(3)(2)^3/12=2$ |
| B | $(1)(3)/2=1.5$ | 1 | -1.33 | 1.5 | 2.65 | $(1)(3)^3/36= 0.75$ | $(3)(1)^3/36= 0.083$ |
| C | $(1)(3)/2=1.5$ | 1 | 1.33 | 1.5 | 2.65 | $(1)(3)^3/36= 0.75$ | $(3)(1)^3/36= 0.083$ |
| D | $-\pi(0.5)^2 = -0.25\pi$ | 1.5 | 0 | -0.5625π | 0 | $-(\pi)(0.5)^4/4 = -0.0156 \pi$ | $-(\pi)(0.5)^4/4 = -0.0156 \pi$ |
| Sum of columns: | | | | 14.73 | 5.3 | 5.95 | 2.118 |

$$I_x = \sum I_{xo} + \sum Ad_x^2 = 20.68 \text{ in}^4$$

$$I_y = \sum I_{yo} + \sum Ad_y^2 = 7.42 \text{ in}^4$$