

## Design and topology optimisation of fractal vasculature

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### Abstract

Fractal patterns develop naturally in vascular systems. The formation of fractal patterns is supposedly driven by self-optimisation to maximise transportation rate. To test this hypothesis, we have formulated a vasculature design problem as a topology optimisation problem with diffusion criterion. Solid isotropic material with penalisation (SIMP) method was employed to optimise two-dimensional model, which consisted of a fluid phase that had a high diffusivity and a solid phase that had a low diffusivity. A range of optimised vascular designs had been thereafter obtained by using different fluid and solid diffusivity values. It was found that with a very low solid diffusivity, the optimised fluid phases resemble natural vascular systems and exhibit certain degree of fractality. Increasing solid diffusivity or increasing surface flux at the modelling boundary reduced the resultant fractality. The link between optimality and fractality was found to be case-specific, generally associated with low diffusivity, high volumetric force, and low surface flux.

**Keywords:** Diffusion optimisation, Fractal, Artificial Vasculature